Name: Feedback

SA402 · Dynamic and Stochastic Models

Quiz 5 – 10/4/2023

Instructions. You have 10 minutes to complete this quiz. You may use your plebe-issue TI-36X Pro calculator. You may <u>not</u> use any other materials.

Show all your work. To receive full credit, your solutions must be completely correct, sufficiently justified, and easy to follow.

Problem 1. Let $Y \sim \text{Poisson}(5)$. Compute $\Pr\{Y > 3\}$.

See Problem 1c from the Lesson 8 Exercises for a similar example.

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| Problem | Weight | Score |
|---------|--------|-------|
| 1 | 1 | |
| 2 | 1 | |
| 3 | 1 | |
| 4 | 1 | |
| Total | | / 40 |

Problem 2. Let $Y \sim \text{Poisson}(73)$. Compute E[Y].

See Problem 1d from the Lesson 8 Exercises for a similar example.

Problem 3. Let $T \sim \text{Erlang}(6, 1/2)$. Compute $\Pr\{T \leq 2\}$.

See Problems 3a and 3c from the Lesson 8 Exercises for similar examples. Note that in this problem, you are being asked for $Pr{T \le 2}$, which is slightly different from these examples.

Problem 4. Let $G \sim \text{Exponential}(1/5)$. Compute $\Pr\{4 < G < 6\}$.

See Problems 2a and 2b from the Lesson 8 Exercises for similar examples.

Note that G is a continuous random variable, so

$$\Pr\{4 < G < 6\} = \Pr\{4 \le G < 6\} = \Pr\{4 \le G \le 6\} = \Pr\{4 \le G \le 6\} = \Pr\{4 \le G \le 6\}$$

| | $X \sim \text{Poisson}(\mu)$ | $X \sim \operatorname{Exponential}(\lambda)$ | $X \sim \operatorname{Erlang}(n, \lambda)$ |
|-------------------|---|---|---|
| pmf / pdf | $p_X(a) = \begin{cases} \frac{e^{-\mu}\mu^a}{a!} & \text{if } a = 0, 1, 2, \dots \\ 0 & \text{o/w} \end{cases}$ | $f_X(a) = \begin{cases} \lambda e^{-\lambda a} & \text{if } a \ge 0\\ 0 & \text{o/w} \end{cases}$ | $f_X(a) = \begin{cases} \frac{\lambda(\lambda a)^{n-1}e^{-\lambda a}}{(n-1)!} & \text{if } a \ge 0\\ 0 & \text{o/w} \end{cases}$ |
| cdf | $F_X(a) = \sum_{k=0}^{\lfloor a \rfloor} \frac{e^{-\mu} \mu^k}{k!}$ | $F_X(a) = \begin{cases} 1 - e^{-\lambda a} & \text{if } a \ge 0\\ 0 & \text{o/w} \end{cases}$ | $F_X(a) = \begin{cases} 1 - \sum_{k=0}^{n-1} \frac{e^{-\lambda a} (\lambda a)^k}{k!} & \text{if } a \ge 0\\ 0 & \text{o/w} \end{cases}$ |
| expected value | $E[X] = \mu$ | $E[X] = \frac{1}{\lambda}$ | $E[X] = \frac{n}{\lambda}$ |
| variance | $\operatorname{Var}(x) = \mu$ | $\operatorname{Var}(X) = \frac{1}{\lambda^2}$ | $\operatorname{Var}(X) = \frac{n}{\lambda^2}$ |